

3.

$$f(x, y) = \begin{cases} k(2x+y) & \forall x \in [0, 1] \text{ and } y \in [0, 1] \\ 0 & \text{otherwise} \end{cases}$$

$$\begin{aligned} \int_{0.5}^1 dy \int_0^1 dx f(x, y) &= \int_{0.5}^1 dy \int_0^1 dx k(2x+y) = k \int_{0.5}^1 dy \left(2 \frac{x^2}{2} + yx \right) \Big|_{x=0}^{x=1} \\ &= k \int_{0.5}^1 dy (1+y) = k \left[y + \frac{y^2}{2} \right]_{y=0.5}^{y=1} \\ &= k \left\{ \left(1 + \frac{1}{2} \right) - \left(\frac{1}{2} + \frac{(\frac{1}{2})^2}{2} \right) \right\} = k \left\{ \frac{3}{2} - \left(\frac{4}{8} + \frac{1}{8} \right) \right\} \\ &= k \left\{ \frac{12}{8} - \frac{5}{8} \right\} = k \frac{7}{8} \end{aligned}$$

$$\begin{aligned} \int_{-\infty}^{\infty} dy \int_{-\infty}^{\infty} dx f(x, y) &= \int_{-\infty}^0 dy \int_{-\infty}^0 dx f(x, y) + \int_0^1 dy \int_{-\infty}^{\infty} dx f(x, y) + \int_1^{\infty} dy \int_{-\infty}^{\infty} dx f(x, y) \\ &= \int_{-\infty}^0 dy \int_{-\infty}^0 dx 0 + \int_0^1 dy \int_{-\infty}^{\infty} dx f(x, y) + \int_1^{\infty} dy \int_{-\infty}^{\infty} dx 0 \\ &= \int_0^1 dy \int_{-\infty}^0 dx f(x, y) + \int_0^1 dy \int_0^1 dx f(x, y) + \int_0^1 dy \int_1^{\infty} dx f(x, y) \\ &= \int_0^1 dy \int_{-\infty}^0 dx 0 + \int_0^1 dy \int_0^1 dx k(2x+y) + \int_0^1 dy \int_1^{\infty} dx 0 \\ &= \dots \end{aligned}$$