Nitrate Variability in Groundwater of North Carolina using Monitoring and Private Well Data Models

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Supporting Information

ABSTRACT: Nitrate (NO$_3^-$) is a widespread contaminant of groundwater and surface water across the United States that has deleterious effects to human and ecological health. This study develops a model for predicting point-level groundwater NO$_3^-$ at a state scale for monitoring wells and private wells of North Carolina. A land use regression (LUR) model selection procedure is developed for determining nonlinear model explanatory variables when they are known to be correlated. Bayesian Maximum Entropy (BME) is used to integrate the LUR model to create a LUR-BME model of spatial/temporal varying groundwater NO$_3^-$ concentrations. LUR-BME results in a leave-one-out cross-validation $r^2$ of 0.74 and 0.33 for monitoring and private wells, effectively predicting within spatial covariance ranges. Results show significant differences in the spatial distribution of groundwater NO$_3^-$ contamination in monitoring versus private wells; high NO$_3^-$ concentrations in the southeastern plains of North Carolina; and wastewater treatment residuals and swine confined animal feeding operations as local sources of NO$_3^-$ in monitoring wells. Results are of interest to agencies that regulate drinking water sources or monitor health outcomes from ingestion of drinking water. Lastly, LUR-BME model estimates can be integrated into surface water models for more accurate management of nonpoint sources of nitrogen.

INTRODUCTION

Nitrate (NO$_3^-$) is a widespread contaminant of groundwater and surface water across the United States that has deleterious effects to human and ecological health. The maximum contaminant level of 10 mg/L established by the U.S. Environmental Protection Agency was based on the prevention of methemoglobinemia in infants; moreover, there is concern of many cancer types and from lower concentration exposures. Excessive NO$_3^-$ inputs into the environment can result in adverse changes to ecosystems such as eutrophication and harmful algal blooms.

Protection of drinking water sources is mandated by the Safe Drinking Water Act; however, private well drinking water is unregulated in contrast to regulated public water systems. In North Carolina where more than 1/4 of the population relies on private wells for drinking water, quantifying potential exposures is important to protect public health. Monitoring programs such as the U.S. Geological Survey’s (USGS) National Water Quality Assessment (NAWQA) Program and the NC Division of Water Resources (NC DWR) ambient monitoring program are effective because they use consistent sampling and analytical methods, yet this water quality monitoring data is spatially and temporally sparse.

Land use regression (LUR) is a proven method that complements monitoring programs and provides effective means for water quality exposure assessments. Previous studies have related land use characteristics to NO$_3^-$ contamination in surface waters and groundwater. Additionally, regression-based methods have been implemented for estimating loading to surface waters. In North Carolina, groundwater discharge to streams (baseflow) accounts for roughly two-thirds of annual streamflow in the Coastal Plains region of North Carolina and may be contributing excess nutrient loads in streams; however, current surface water models do not directly account for this large source of NO$_3^-$ from baseflow.

For linear regression models, traditional statistical methods to select predictor variables include forward, backward, and stepwise selection. These methods can lead to erroneous models with high multicollinearity when the candidate variables are related. However, for LUR model studies, model selection methods have been modified to accommodate the potential high multicollinearity from selection variables that differ only by...
a hyperparameter.\cite{16,19} Additionally, lasso\cite{28} and elastic net\cite{29} regression are potential methods for selecting linear LUR models, but to the authors’ knowledge has not been employed for LUR model selection. For nonlinear regression, methods for model selection based on a large candidate variable space include stepwise logistic regression\cite{30,31} and regression tree analysis which approximates nonlinear relationships;\cite{32,33} still for continuous variable outcomes with nonlinear models, less rigorous methods for model selection have been developed. The number of candidate variables is generally consolidated to a tractable number through expert knowledge or single variable regression, and then various combinations of models are tested until one finds the best model in terms of a validation statistic like $R^2$ or Akaike Information Criterion (AIC).\cite{15,21,24}

The advanced geostatistical method of Bayesian Maximum Entropy (BME) has also been shown to successfully estimate groundwater quality contaminants.\cite{19,24} An advantage of BME is its ability to quantify spatial and temporal variability which is then used in the estimation process at unmonitored locations. BME, like all geostatistical methods, is data driven and can only provide reliable estimates within the vicinity of measured values. However, BME utilizes Bayesian epistemic knowledge blending to combine multiple sources of data, which has been successfully demonstrated with incorporation of deterministic mean trend functions into BME for groundwater.\cite{19}

Local spatial and temporal variability have lead previous studies to reduce NO$_3^−$ variability with a combination of spatial smoothing and temporal averaging.\cite{15,35,36} For instance, Nolan and Hitt spatially smoothed NO$_3^−$ by taking watershed averages over their study time period, based on watersheds with an average size of approximately 2000 square-kilometers. They not only helped elucidate trends and potential explanatory variables, but they were able to explain a large percentage in the variability of spatially smoothed NO$_3^−$ with a $R^2$ of 0.80 for shallow aquifer NO$_3^−$ and 0.77 for deep aquifer NO$_3^−$ However, this advantage of reducing groundwater NO$_3^−$ variance is also a limitation because factors affecting spatially smoothed and temporally averaged NO$_3^−$ might not affect point-level NO$_3^−$ and vice versa. Furthermore, since groundwater NO$_3^−$ contains significant local variability, the need to provide local estimates of its variability naturally follows. Models developed for predicting spatially smoothed and temporally averaged NO$_3^−$ will likely not be successful in predicting observed, point-level NO$_3^−$.

The objectives of this study are to (1) develop a novel nonlinear regression model for spatial point-level and time-averaged groundwater NO$_3^−$ concentrations in monitoring and private wells of North Carolina, (2) produce the first space/time estimates of groundwater NO$_3^−$ concentrations across a large study domain by integrating LUR models into the BME framework, and (3) compare space/time NO$_3^−$ concentration models to the current standard of spatially averaged NO$_3^−$ concentration models. Two nonlinear models, whose form is adopted from Nolan and Hitt\cite{15} with components that represent NO$_3^−$ sources, attenuation, and transport, are created and selected with a new model selection framework for nonlinear regression models with correlated explanatory variables. We then integrate the LUR models into the BME framework to model space/time point-level NO$_3^−$. Results are of interest to agencies that regulate drinking water sources or that monitor health outcomes from ingestion of drinking water. Additionally, the results can provide guidance on factors affecting the point-level variability of groundwater NO$_3^−$ and new resources for more accurate management of NO$_3^−$ loads.

### MATERIALS AND METHODS

**Nitrate Data.** NO$_3^−$ data across North Carolina are obtained from three data sources (Supporting Information (SI) Figure S1), which are detailed as follows:

- North Carolina Division of Water Resources (NC-DWR) collects data near select permitted, dedicated wastewater treatment residual (WTR) application fields via monitoring wells. The second source is U.S. Geological Survey (USGS) data obtained through the National Water Information System (NWIS). Well depth information is not linked directly to each monitoring well although a subset of well depth information is available. Based on the subset with depth information, they have a mean depth of 33 feet with a standard deviation of 32 feet. Together, the NCDWR and USGS data represent shallow aquifer monitoring wells ($n = 12,322$), which hereafter will be referred to as “monitoring well data.”

- The last data set of groundwater NO$_3^−$ comes from private well data collected by the North Carolina Department of Health and Human Services (NC-DHHS). Groundwater NO$_3^−$ was obtained and address geocoded using the same process outlined in Messier et al.\cite{19} Well depth information is not linked to water quality measurements, but a separate database on private well construction contains well depths. The mean depth is 95 feet with a standard deviation of 109 ft. This data will hereafter be referred to as “private well data” and this data is assumed to represent a deeper aquifer model of groundwater NO$_3^−$ ($n = 22,067$).

The median NO$_3^−$ concentrations for the NC-DWR, USGS, and private well data are 1.30, 0.10, and 0.62 mg/L respectively. The means are 4.61, 6.14, and 1.66 mg/L respectively. The percent observed above the detection limit is 79.7, 61.4, and 30.6 respectively. Additional basic statistics for the data set are available in the SI (Table S1).

**Spatial and Temporal Observation Scales.** In this work we develop models for NO$_3^−$ at three observation scales. The finer scale corresponds to the space/time point-level NO$_3^−$ data, that is, NO$_3^−$ data as it is sampled. An intermediate observation scale corresponds to the time-averaged data, whereby NO$_3^−$ at each well is averaged. The time-averaged data provides point-level spatial resolution, but no time variability. Finally, the coarser resolution observation scale corresponds to the spatially smoothed/time-averaged data, which was obtained by spatially smoothing the time-averaged data using a 25 km exponential kernel function. We choose 25 km as it is approximately the average size of watersheds in many NAWQA groundwater studies.\cite{15,37} While previous works over large study domains have developed models for spatially smoothed/time average NO$_3^−$ data, very few models, if any, have been developed for point-level NO$_3^−$ data over large study domains. Our work therefore fills that knowledge gap.

**Maximum Likelihood Estimation of Nitrate Distributions.** Our notation for variables denotes a single random variable $Z$ in capital letter, its realization, $z$, in lower case; and vectors and matrices in bold faces, for example, $Z = [Z_1,...,Z_n]^T$ and $Z = [z_1,...,z_n]^T$.

Due to the high percentage of nondetect (left-censored) data in both the monitoring well and private well databases, a maximum likelihood estimation (MLE) is used for the estimation of monitoring well and private well distribution parameters,\cite{38} which is assumed to follow a log-normal.
distribution. MLE can directly account for the nondetect values by modifying the likelihood equation, with the censored observations given by the cumulative distribution function (CDF) evaluated at the detection limit. The MLE equation then becomes

\[ L(\mu, \sigma) = \left\{ \prod_{z_i \leq t_i} f_{\mu,\sigma}(z_i) \right\} \times \left\{ \prod_{z_i > t_i} F_{\mu,\sigma}(t_i) \right\} \]

where \( f_{\mu,\sigma}(z) \) denotes the normal probability distribution function (PDF) of log-transformed (natural log) point-level \( NO_3^- \) concentration with mean and standard deviation parameters \( \mu \) and \( \sigma \), and \( F_{\mu,\sigma}(t) \) denotes the CDF of the distribution taken at the log of the detection limit \( t \). The estimated distributions are used to quantify the extent of contamination in monitoring and private wells and to handle nondetect data. For the regression analysis, the log-\( NO_3^- \) concentration of a measurement below detection limit \( t_i \) is assigned a value equal to the mean of the normal distribution \( N(\mu,\sigma) \) truncated above \( \log(t_i) \), whereas the geostatistical analysis can handle the full truncated normal distribution.

**Spatial Explanatory Variables.** Spatial explanatory variables representing possible groundwater \( NO_3^- \) sources, attenuation, and transport factors were constructed prior to model development. Potential variables are summarized below with details available in the SI (Table S2).

All of the explanatory variables have an inherent spatial distance parameter such as circular buffer radius or exponential decay range, which hereinafter is referred to as the hyperparameter. Each variable is calculated with multiple hyperparameter values since optimal distance is unknown a priori. In the final model selection process, a maximum of one hyperparameter value is allowed to be selected from each variable to avoid multicollinearity and effectively optimize the hyperparameter. The following variables adopted from Nolan and Hitt\textsuperscript{15} are \( NO_3^- \) sources calculated as kg-\( NO_3^- /yr/ha \) within a circular buffer: Sources include farm fertilizer, nonfarm fertilizer, manure, and \( NO_3^- \) atmospheric deposition. Each National Landcover Database (NLCD) category is calculated as a percent within a circular buffer. On-site wastewater treatment plant variables, septic density and average nitrate loading, are created following the methods of Pradhan et al.\textsuperscript{19} The following point sources are calculated as the sum of exponentially decaying contributions:\textsuperscript{19} Wastewater treatment residual field application sites (WTR), swine confined animal feeding operations (CAFOs), poultry CAFOs, cattle farms, and wastewater treatment plants (WWTP). Mean slope in degrees and topographic wetness index\textsuperscript{40} (TWI) are calculated within circular buffers. Water withdrawals in cubic meters per second are calculated using USGS water use estimates.\textsuperscript{11} Lastly, population density is calculated within circular buffers from U.S. Census block data assuming an even distribution of population per census block.

**Nonlinear Regression Model Selection.** In order to develop a LUR model for \( NO_3^- \) we adopt a similar nonlinear multivariable model implemented by groundwater vulnerability assessment (GWAVA)\textsuperscript{15} which is also similar to the surface water counterpart spatially referenced regression on watershed attributes (SPARROW).\textsuperscript{21,23,24} We partition explanatory variables into source, attenuation, and transport terms. Following Nolan and Hitt,\textsuperscript{15} the nonlinear multivariable model is constructed as follows:

\[
z_i = \beta_0 + \left\{ \sum_{k=1}^{E-1} \beta_k Y_i^{(k)}(\lambda_k) \right\} \exp\left\{ \sum_{l=1}^{M} -\delta Y_i^{(l)}(\lambda_m) \right\} \exp\left\{ \sum_{m=1}^{M} \delta Y_i^{(m)}(\lambda_m) \right\} + \epsilon_i
\]

where \( z_i \) is the log-transform of \( NO_3^- \) concentration at point \( i \), \( \beta_0 \) is the intercept, \( Y_i^{(k)}(\lambda_k) \) is the \( k \)-th source predictor variable at point \( i \) with hyperparameter value \( \lambda_k \), \( \lambda_k \) is its regression coefficient, \( Y_i^{(l)}(\lambda_l) \) is the \( l \)-th attenuation predictor variable at point \( i \) with hyperparameter value \( \lambda_l \) \( \gamma_l \) is its attenuation regression coefficient, \( Y_i^{(m)}(\lambda_m) \) is the \( m \)-th transport predictor variable with hyperparameter value \( \lambda_m \) \( \delta_m \) is its transport regression coefficient, and \( \epsilon_i \) is an error term. The model contains an additive, linear submodel for sources, and multiplicative exponential terms for the attenuation and transport variables that act directly on the source terms.\textsuperscript{15} For example \( Y_i^{(k)}(\lambda_k) \) may be equal to a land cover variable or a point source variable. The attenuation variables, \( Y_i^{(l)}(\lambda_l) \), physically represent areas that are associated with removing \( NO_3^- \) from groundwater such as wetlands and histosol soil. The transport variables, \( Y_i^{(m)}(\lambda_m) \), may be equal to any variable that affects the movement of \( NO_3^- \) in the groundwater such as the soil permeability and average slope. The attenuation variable coefficients, \( \gamma_l \), are constrained to be negative allowing them to only decrease \( NO_3^- \) concentrations, while the transport variable coefficients, \( \delta_m \), are unconstrained allowing variables to increase or decrease \( NO_3^- \) concentrations.

We developed a nonlinear model regression model selection technique that accommodates variables that differ only by a hyperparameter and can be adapted for various nonlinear model forms. Our model selection procedure is essentially a nonlinear extension of a distance decay regression selection strategy (ADDRESS)\textsuperscript{16} since to the authors’ knowledge there is not a regression selection strategy for nonlinear LUR. We implement constrained forward nonlinear regression with hyperparameter optimization (CFN-RHO) whose simple algorithm is as follows (SI Figure S2):

1. **Initialization:** Linear regression on all candidate variables to obtain the initial values for the nonlinear model fitting.
2. **Candidate Variables:** In the first iteration, the candidate variables consist of the source variables only. In the second iteration, candidate variables consist of attenuation and transport variables only. This is done so as to obtain an initial model with at least one source and one attenuation or transport variable. In every iteration afterward the candidate variables can be any variable.
3. **Nonlinear Regression:** Nonlinear regression is performed by adding each candidate variable to the current model one at a time. Note that candidate variables are added according to their predetermined place in the nonlinear model (i.e., Source variables are in a linear submodel; Attenuation and transport in the exponential submodel.).
4. **Variable Selection:** The variable that results in the highest R-Squared (lowest AIC is also an option) while constrained to maintaining all variables in the model statistically significant (p-value <0.05), is selected and added to the model. R-Squared ties beyond the thousandth decimal place are settled by the lowest p-value.
5. **Hyperparameter Optimization:** The rest of the candidate variables that differ from the selected variable by only a
To improve estimation accuracy, we integrate the spatiotemporal geostatistics. For more detailed derivations of BME equations and empirical relationships, non-Gaussian distributions, hard and soft data, etc., we refer the reader to other works for more detailed derivations of BME equations and LUR integration into BME.

**BME Estimation Framework for Space/Time Mapping Analysis.** To improve estimation accuracy, we integrate the time-averaged LUR results into the bayesian maximum entropy (BME) method of modern spatiotemporal geostatistics. BME is a space/time geostatistical estimation framework grounded in epistemic principles that reduces to the space/time simple, ordinary, and universal Kriging methods as its knowledge is organized in the general knowledge base, while also allowing the flexibility to process a wide variety of additional knowledge bases (physical laws, empirical relationships, non-Gaussian distributions, hard and soft data, etc.). We provide the fundamental BME equations for mapping NO3⁻; the reader is referred to other works for more detailed derivations of BME equations and LUR integration into BME.

Let Z(p) be the space/time field (S/TRF) describing the distribution of ground water log-NO3⁻ across space and time, where p = (s,t), s is the space coordinate and t is time. The knowledge available is organized in the general knowledge base (G-KB) about the space/time trend and variability (e.g., mean, covariance) of NO3⁻ across the study domain, and the site-specific knowledge base (S-KB) corresponding to the hard and soft data zₖ available at a set of specific space/time points pₖ.

First, we define the transformation of log-NO₃⁻ data zₖ at locations pₖ as

\[ xₖ = zₖ - oₖ(pₖ) \]  

where \( oₖ(pₖ) \) may be any deterministic offset that can be mathematically calculated at any space/time coordinate \( p \). We then define X(p) as a homogeneous/stationary S/TRF representing the variability and uncertainty with the transformed data \( xₖ \) that is, such that \( xₖ \) is a realization of \( X(p) \). Finally we let \( Z(p) = X(p) + oₖ(p) \) be the S/TRF representing ground water log-NO₃⁻. In this study, we consider two choices for \( oₖ(p) \): (1) a constant value determined by the MLE mean resulting in a purely BME model, and (2) the LUR estimate \( L_r(pₖ) \) from CFN-RHO resulting in a LUR-BME model.

The G-KB for the S/TRF \( X(p) \) describes its local space/time trends and dependencies. In this work, the general knowledge consists of the space/time mean trend function \( m_p(p) = E[X(p)] \), and the covariance function \( C_p(p,p') = E[(X(p) - m_p(p))(X(p') - m_p(p'))] \) of the S/TRF \( X(p) \). The S-KB consists of hard data and soft data; with hard data, \( xₖ = zₖ - L_r(pₖ) \) for data points where \( zₖ \) is observed over the detection limit and soft data, \( xₖ \), is at locations \( pₖ \) where NO₃⁻ is observed below the detection limit. Following Messier et al.,^19 the BME soft data for log-NO₃⁻ is modeled as a Gaussian distribution truncated above the log of the detection limit.

The overall knowledge bases considered consist of \( G = \{ m_p(p), C_p(p,p') \} \), and \( S = \{ f(·), X_k \} \). In this case the BME set of equations reduces to

\[ f_K(xₖ) = A^{-1} \int dxₖ f_G(xₖ, xₖ, xₖ)f_S(xₖ) \]  

where \( f_K(xₖ) \) is the BME posterior PDF for the offset-removed log NO₃⁻(xₖ) at some unmonitored estimation point \( pₖ \), \( f_G(xₖ, xₖ, xₖ) \) is the (maximum entropy) multivariate Gaussian PDF for \( (xₖ, xₖ, xₖ) \) with mean and variance-covariance given by G-KB, \( f_S(xₖ) \) is the truncated Gaussian PDF of \( X_k \), and \( A^{-1} \) is a normalizing constant. After the BME analysis is conducted, \( oₖ(p) \) is added back to obtain log-NO₃⁻ concentrations.

**Validation Statistics.** The robustness of CFN-RHO is tested with a 10-fold cross-validation procedure. In 10-fold cross-validation data is randomly partitioned into 10 equal size subsamples. A single subsample is retained as the validation data for testing the model, and the remaining nine subsamples are used as training data. Each of the 10 subsamples is used exactly once as the validation data. Similar variable selections (which may differ only by hyperparameter) for subsamples demonstrate model selection robustness.

Models are compared with a leave one-out cross-validation (LOOCV) mean squared error (MSE) and R-squared. Spatially smoothed/time-averaged NO₃⁻ and time-averaged NO₃⁻ models are also tested on how well they predict at the smaller observation scales. In LOOCV, each log-NO₃⁻ value \( Z_i \) is removed one at a time, and re-estimated using the given model based only on the remaining data. Let \( Z_i^{(k)} \) be the re-estimate

<table>
<thead>
<tr>
<th>method</th>
<th>spatially smoothed/time-averaged NO₃⁻</th>
<th>time-averaged NO₃⁻</th>
<th>point-level NO₃⁻</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MW (n = 951) PW (n = 18,664)</td>
<td>MW (n = 951) PW (n = 18,664)</td>
<td>MW (n = 12,300) PW (n = 22,062)</td>
</tr>
<tr>
<td>spatially smoothed/time-averaged LUR</td>
<td>( r )</td>
<td>0.69</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>RMSE</td>
<td>0.895</td>
<td>0.293</td>
</tr>
<tr>
<td>time-averaged LUR</td>
<td>( r )</td>
<td>0.37</td>
<td>0.09</td>
</tr>
<tr>
<td>space/time BME</td>
<td>( r )</td>
<td>RMSE</td>
<td>2.08</td>
</tr>
<tr>
<td>space/time LUR-BME</td>
<td>( r )</td>
<td>RMSE</td>
<td>0.70</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.39</td>
<td>1.23</td>
</tr>
<tr>
<td></td>
<td></td>
<td>0.74</td>
<td>0.33</td>
</tr>
<tr>
<td></td>
<td></td>
<td>1.27</td>
<td>1.08</td>
</tr>
</tbody>
</table>

"Note that methods were used to predict at scales more refined or equal to its calibration scale. MW = Monitoring Well model. PW= Private Well model. n = number of observations at that scale. Time averaging results in fewer observations. RMSE = root mean squared error. Units of NO₃⁻ concentration = mg/L."
**Table 2. Nonlinear Regression Model Variables Selected via CFN-RHO and Parameter Estimates for Time-Averaged NO$_3^-$ Monitoring (Left) and Private Well (Right) Models$^a$**

<table>
<thead>
<tr>
<th>variable</th>
<th>monitoring well</th>
<th>variable range</th>
<th>coefficient estimate</th>
<th>standard error</th>
<th>private well</th>
<th>variable range</th>
<th>coefficient estimate</th>
<th>standard error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant</td>
<td></td>
<td>n/a</td>
<td>-3.71</td>
<td>0.191</td>
<td></td>
<td>n/a</td>
<td>-1.570</td>
<td>0.0382</td>
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<tr>
<td>Source Variables</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>manure$^a$</td>
<td></td>
<td>250 m</td>
<td>0.0759</td>
<td>0.0317</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>wastewater treatment residuals (WTR)$^b$</td>
<td></td>
<td>5 km</td>
<td>0.245</td>
<td>0.0274</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>farm fertilizer$^a$</td>
<td></td>
<td>250 m</td>
<td>0.132</td>
<td>0.0193</td>
<td></td>
<td>250 m</td>
<td>0.0432</td>
<td>0.0025</td>
</tr>
<tr>
<td>swine CAFO$^c$</td>
<td></td>
<td>2 km</td>
<td>0.117</td>
<td>0.0218</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>swine lagoons$^b$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>6 km</td>
<td>0.1079</td>
<td>0.0146</td>
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<tr>
<td>developed low$^d$</td>
<td></td>
<td>250 m</td>
<td>0.112</td>
<td>0.0214</td>
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<td></td>
<td></td>
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<tr>
<td>developed (all combined)$^d$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>100 m</td>
<td>0.0112</td>
<td>7.08e-4</td>
</tr>
<tr>
<td>atmospheric deposition$^a$</td>
<td></td>
<td>250 m</td>
<td>0.477</td>
<td>0.129</td>
<td></td>
<td>25 km</td>
<td>2.94e-11</td>
<td>2.53e-10</td>
</tr>
<tr>
<td>forest (all combined)$^d$</td>
<td></td>
<td>2 km</td>
<td>-0.0064</td>
<td>0.00281</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>deciduous forest$^c$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>4 km</td>
<td>-0.0151</td>
<td>0.00127</td>
</tr>
<tr>
<td>herbaceous wetlands$^c$</td>
<td></td>
<td>5 km</td>
<td>-0.531</td>
<td>0.079</td>
<td></td>
<td>25 km</td>
<td>-0.106</td>
<td>0.0126</td>
</tr>
<tr>
<td>histosol$^d$</td>
<td></td>
<td>25 km</td>
<td>-0.0427</td>
<td>0.0111</td>
<td></td>
<td>500 m</td>
<td>-0.012</td>
<td>0.0010</td>
</tr>
<tr>
<td>hydrologic soil group$^c$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>slope$^e$</td>
<td></td>
<td>25 km</td>
<td>-0.074</td>
<td>0.0261</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

$^a$All variables are significant with $p$-value < 0.025. Variables units: a, kg-N0$_3^-$/yr/ha; b, dimensionless; c- 100 pigs; d, percent; e, degrees; (−) not a variable in the model.

for method $k$ then $MSE^{(k)} = (1/n) \sum_{i=1}^{n} (Z_i^{(k)} - Z_i)^2$ and the cross-validation R-Squared is $R^2(Z,Z^{(k)})$.

**RESULTS**

**Nitrate Concentrations.** The MLE of the statewide monitoring concentrations resulted in a geometric mean and standard deviation of the log-normal distribution of 0.62 and 14 mg/L, respectively (SI Figure S3). MLE for private wells resulted in a geometric mean and standard deviation of 0.45 and 5.1 mg/L (SI Figure S3).

**Spatially Smoothed/Time-Averaged Nitrate.** The 25 km spatially smoothed/time-averaged NO$_3^-$ LUR model cross-validation results (Table 1) in a $r^2$ of 0.69 and 0.68 for monitoring and private wells, respectively, which is of similar magnitude to current literature. However, as expected, the LUR model calibrated for spatially smoothed/time-averaged NO$_3^-$ underperforms and does progressively worse (top row, moving left to right in Table 1) as it predicts time-averaged NO$_3^-$ and point-level NO$_3^-$ with lower $r^2$ and higher RMSE. The variables selected for this model via CFN-RHO are available in the SI (Table S3).

10-fold cross-validation of spatially smoothed/time-averaged NO$_3^-$ LUR models was done to demonstrate the stability of CFN-RHO (SI Tables S4, S5). All variables were selected 7 and 10 out of 10 iterations for the monitoring and private well models, respectively.

**Time-Averaged Nitrate.** The LUR variables selected through CFN-RHO for time-averaged NO$_3^-$ observed at monitoring wells and private wells are shown in Table 2. The LUR calibrated to predict time-averaged NO$_3^-$ obtained a $r^2$ of 0.37 and 0.09 for monitoring wells and private wells, respectively (Table 1, second row). Moreover, the LUR model predicts point-level NO$_3^-$ with a $r^2$ of 0.23 and 0.09 for monitoring and private well, respectively. LUR maps are available in SI Figure S4.

10-fold cross-validation of time-averaged NO$_3^-$ LUR models was conducted (SI Table S6, S7). All variables selected from the monitoring well model are selected in at least six iterations of the 10-fold cross-validation runs. The majority of variables in the private well model were also stable; however swine lagoons and deciduous forest were only selected 2 and 0 out of 10 times. In both models, when a variable is not selected in the 10-fold cross validation it is likely due to other variables that capture similar source, attenuation, or transport processes (i.e., Forest instead of Deciduous, Swine CAFO’s instead of Swine Lagoons).

**Point-Level Nitrate.** We modeled the space/time covariance of the LUR offset removed log-NO$_3^-$ S/TRF, $X(p)$, using a two-component, space/time nonseparable, exponential covariance model following Messier et al.\textsuperscript{19}:

$$C_X(r, \tau) = c_1 \exp \left( -\frac{3\tau}{a_1} \right) \exp \left( -\frac{3\tau}{a_2} \right) + c_2 \exp \left( -\frac{3\tau}{a_3} \right)$$

where $c_1 = 0.67$ (log – mg/L)$^2$, $a_1 = 93$m, $a_2 = 15 days$, $c_2 = 3.6$ (log-mg/L)$^2$, $a_2 = 1750$m, $a_3 = 15840$ days for monitoring wells (SI Figure S5) and a one-component, space/time exponential covariance model for private well where $c_1 = 0.76$ (log – mg/L)$^2$, $a_1 = 181$m, $a_2 = 8640$ days (SI Figure S6).

The LUR-BME model, which integrates the time-averaged LUR as the offset best predicts space/time point-level NO$_3^-$ concentrations with a $r^2$ of 0.74 and 0.33 (Table 1) for monitoring and private wells, respectively. However, the LUR-BME predictions have a large variance at locations farther than the covariance model spatial range. Figure 1 maps the point-level NO$_3^-$ concentrations estimated by LUR-BME for 1 day during the study period for both monitoring and private well models. These are the first results to show that there is a 4-fold improvement in predicting point-level NO$_3^-$ when the LUR-BME method is used in comparison to previous studies that use
models for spatially smoothed/time-averaged NO$_3^-$, and five percent improvement in $r^2$ when integrating a LUR model into the BME framework, over purely BME. A link to a movie of LUR-BME maps is available in the SI.

**DISCUSSION**

**Groundwater Nitrate Maps.** This study presents a LUR model for point-level NO$_3^-$ in North Carolina that elucidates processes affecting its local variability, and then utilizes the strengths of BME to create the first LUR-BME model of groundwater nitrate’s spatial/temporal distribution including prediction uncertainty. The first major finding is the LUR-BME model for monitoring wells, assumed to represent surficial aquifers, (Figure 1, SI Movie S1) shows groundwater NO$_3^-$ that is highly variable with many areas predicted above the current standard of 10 mg/L.
Contrarily, the private well results (Figure 1) depict widespread, low-level NO$_3^-$ concentrations, which is consistent with the current physical understanding in which sources tend to pollute the surficial aquifer, but then transport over time to the deeper drinking-water supply aquifers where concentrations are lower. This finding is significant because of the studies demonstrating potential significant health effects at concentrations as low as 2.5 mg/L. Additionally, concentrations of NO$_3^-$ could impact ecological function since there are potential large reserves in deeper aquifers that can discharge to surface waters. The standard deviation maps (Figure 1) demonstrate the importance of NC-DWR and USGS monitoring wells and private well testing because areas within the spatial covariance range are well characterized, whereas those outside are less reliable.

The second major finding is the LUR-BME maps (Figure 1) show that groundwater NO$_3^-$ in monitoring wells is elevated in the southeastern plains of North Carolina (SI Figure S7) due to the larger amount of NO$_3^-$ sources and the lack of subsurface attenuation factors (SI Movie S2) that are present in the coastal plain region. This corroborates the findings of Nolan and Hitt, which also show spatially smoothed/time-averaged NO$_3^-$ to be the highest in the southeastern plains of North Carolina. This expands that finding with point-level results showing significant point-level variability within regional trends. Additional concerns arise since groundwater flow of the southeastern plains contributes significantly to surface water flow.

Our LUR-BME model can be used with surface water models to quantify the effect of groundwater NO$_3^-$ contributing to surface water contamination. The use of the methods in this study provide estimates at a finer resolution and down to smaller NO$_3^-$ values than Nolan and Hitt, resulting in new findings. Nolan and Hitt generally show greater concentrations than the LUR-BME model potentially due to their model using significantly less training data and averaging NO$_3^-$ over watersheds. Our LUR-BME models benefit from the large amount of monitoring ($n = 12,322$) and private well ($n = 22,067$) data, whereas they used 2306 and 2490 across the U.S. for their shallow and drinking water models, respectively.

LUR-BME benefits from the exactitude property of BME, thus our model results are in 100% agreement at monitoring locations. Contrarily, when our observed data is compared with Nolan and Hitt by grouping results according to the bins of Figure 1, Nolan and Hitt overpredicts 48% and 59% of the time for monitoring and private wells, respectively (SI Figure S8, S9). As a result of the finer resolution of our maps and their improved ability to predict low level NO$_3^-$, our results lead to a significant new finding about the extent of areas with low level contamination. Our results show private well concentrations are greater than 0.25 mg/L while monitoring well concentrations are less than 0.25 mg/L in 30.6% of North Carolina’s area, compared to 2.6% for Nolan and Hitt (SI Table S8, S9). Likewise, our results show monitoring and private wells are both above or below 0.25 mg/L at the same location in 68% of North Carolina, compared to 91% for Nolan and Hitt. Hence whereas Nolan and Hitt results suggest the geographical extent of the low level contamination of drinking water aquifer is limited to that of the shallow aquifer, which is consistent with downward transport of NO$_3^-$, our LUR-BME models show that in fact the geographical extent of the contamination of the drinking water extends over a much larger area than that of the shallow aquifer. This major new finding provides new evidence indicating that in addition to downward transport, there is also a significant outward transport of groundwater NO$_3^-$ in the drinking water aquifer to areas outside the range of sources. This is especially significant because it indicates that the deeper aquifers are acting as a reservoir that is not only deeper, but also wider than the reservoir formed by the shallow aquifers.

### LUR Variable Interpretations

Variables selected through CFN-RHO show processes influencing monitoring well and private well NO$_3^-$ concentrations. Interpretations of regression sources parameters are based on the nonlinear model formulation: Since NO$_3^-$ was log-transformed and the nonlinear model has multiplicative interaction, the percent increase of the geometric mean of NO$_3^-$ is the exponential of the coefficient multiplied by the result of the attenuation and transport terms held to their mean value. For instance, in the monitoring well model, the percent increase in the geometric mean of NO$_3^-$ in mg/L for every 1 kg/yr/ha of farm fertilizer is $\exp(0.132 \times 0.456) = 1.06 = 5\%$ where 0.456 is the exponential of the mean attenuation and transport variables multiplied by their coefficients. For the private well model, the percent increase in the geometric mean of NO$_3^-$ for every 1 kg/yr/ha of farm fertilizer is $\exp(0.0432 \times 0.4636) = 1.02 = 2\%$. Every other source coefficient interpretation for time-averaged NO$_3^-$ is provided in the SI.

Comparing variables selected between the spatially smoothed/time-averaged NO$_3^-$ LUR and the time-averaged NO$_3^-$ LUR help elucidate effects the spatial scale has on groundwater NO$_3^-$ concentrations. The variable hyperparameters selected by CFN-RHO help elucidate potential scales at which the variables affect groundwater NO$_3^-$ concentrations. For example, the short buffer range of developed low likely captures the small size of single-family housing yards and their associated fertilizer applications. The monitoring well model WTR has an exponential decay range of 5 km. A possible explanation of this medium range is due to the volatization of NO$_3^-$ into the air, which can then be transported over longer distances than subsurface transport mechanisms alone. Long buffer ranges for attenuation and transport variables such as percent histosol soil and mean slope represent variables with larger, regional scale effects.

The third major finding is that both wastewater treatment residuals (WTR) and swine CAFOs were selected as local sources of groundwater NO$_3^-$ contamination, which to our knowledge have not yet been previously identified as sources in multivariable models that included regional sources. To help aide state-wide policy decisions concerning regional versus local sources, Figure 2 shows the elasticity of LUR predicted sources in monitoring wells, or the percent change in the geometric mean of groundwater NO$_3^-$ within an area in response to the percent decrease in a LUR model source given all other sources remain at current levels. Farm fertilizer and atmospheric deposition result in the greatest decrease in groundwater NO$_3^-$ state-wide (Figure 2A). Reducing WTR (Figure 2B) and swine CAFOs (Figure 2C) within 1 km of the source leads to significant reductions in groundwater NO$_3^-$ in the local area surrounding the sources, demonstrating the importance of sources on local area NO$_3^-$ variability.

### Recommendations and Limitations

This work represents the first step in the development of modeling observed NO$_3^-$ over large domains without averaging. In previous studies, spatial averaging was utilized because it provides results at the domain (state, regional, or national) desired for policy making.
decisions and sheds light on processes influencing groundwater NO$_3$\textsuperscript{-}. We demonstrated that a LUR at the point-level in space is currently limited in terms of model predictive capability but when integrated into the BME framework, the improved model can estimate within the spatial covariance range similar to LUR models for spatially smoothed/time-averaged groundwater NO$_3$\textsuperscript{-} concentrations. Potential explanatory variables that can explain the remaining variability in the point-level LUR will need primary data collection. For instance, we found WTR to be a significant variable even though we just used location of fields. If records of timing and amounts of WTR applications were improved, then the temporal variability in monitoring wells near WTR application fields could be improved. Similarly, a parcel-level query of farm fertilizer application practices could distinguish farms that use NO$_3$\textsuperscript{-} fertilizers efficiently versus farms that apply excessively or with poor timing. For private wells, the short spatial autocorrelation range may be due to differences in effectiveness of on-site wastewater treatment systems or residential fertilizer use. Additionally, we note that candidate variables not selected via CFN-RHO does not necessarily indicate they have no effect on groundwater NO$_3$\textsuperscript{-} concentrations in surficial or confined drinking-water aquifers of North Carolina. Many factors both statistically and physically can affect the selection such as correlation between candidate variables and local hydrogeology conditions being overwhelmed by larger scale trends. This study lacked well depth for the majority of monitoring and private wells. The monitoring and private well models clearly demonstrate a difference in concentrations based on depth, so well depth could quantify this more explicitly as opposed to categorically as done by this study. Furthermore, pumping rate information was not available for the private well data set thus the effect of local pumping could not be quantified. The USGS water use report\textsuperscript{12} has information on domestic-use water withdrawals; however, it is at the county-scale, based on county populations, and cannot be down-scaled like the agricultural water withdrawals variable, thus it was not included as a candidate variable. Additionally, the detection limit of 1 mg/L for the private well data is high and lowering that detection limit would improve the ability of the model to delineate areas with low level contamination that may act as reservoir to surface water NO$_3$\textsuperscript{-} recharge. The high detection limit is also potentially responsible for the lower $r^2$ in the private well LUR model for time-averaged nitrate because it results in a low dependent variable variance. Predictions of the private well LUR model for time-averaged nitrate are likely biased toward the detection limit; however, the LUR-BME model for private well models likely avoids this bias due to the exactitude property along with the good spatial coverage of private well data across North Carolina. Moreover, greater uncertainty in attenuation processes in deeper aquifers is likely contributing to the lower $r^2$.

In conclusion, a LUR model with a novel model selection procedure can elucidate important predictors of point-level groundwater NO$_3$\textsuperscript{-} in North Carolina monitoring and private wells. The methods are translatable to other study areas in the United States. LUR-BME models can be used to predict spatial/temporal varying groundwater NO$_3$\textsuperscript{-} and provide uncertainty assessments. Further research should integrate groundwater NO$_3$\textsuperscript{-} results into surface water models to determine the extent of groundwater’s contribution to surface water contamination. Lastly, results will be useful in identifying localities of elevated NO$_3$\textsuperscript{-} for increased monitoring.

### ASSOCIATED CONTENT

#### Supporting Information

Additional information as noted in text. This material available free of charge via the Internet at http://pubs.acs.org/.

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**Notes**

The authors declare no competing financial interest.

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